

## Documentation of the MATLAB function ProjLinCoefMV.m

The function's arguments and returned quantities are listed in the help section of the function which is reproduced below.

```
function [prest,prvar,Lincoef] =ProjLinCoefMV(x,G)
% projects time series missing values onto observed for m by n series x
% Uses covariance matrix G of x taken by columns of x giving blocks of size mxm
% Solves for linear coefficients of projection from which missing values are derived
% prest is the original series with missing values replaced by projected values
% prvar has same with zeros except variances in place of missing values
% Lincoeff is same size as G with coeffs of missing values in terms of known, elsewhere zeros
```

To be specific, the given array  $\mathbf{x}$  of size  $m \times n$ , which is determined in the function, has elements  $x_{i,t}$  for  $i = 1 \dots m, t = 1 \dots n$  that contain the values  $x_{i,t}$  of stationary times series with lagged covariances

$$\Gamma_{i,j,k} = \text{Cov}(x_{i,t}, x_{j,t-k}).$$

Any desired (strict) subset of elements of  $\mathbf{x}$  may be set to `NaN` as indicating unknown values to be predicted by the function from the complementary set of elements (which should not be empty).

The square array  $\mathbf{G}$  should then be of size  $mn$  with elements  $\mathbf{G}(i,j)$  that are the elements of the covariance matrix  $G$  of  $X = (x'_1, x'_2, \dots, x'_n)'$  and therefore has elements

$$G_{u,v} = \text{Cov}(x_{i,s}, x_{j,t}) = \Gamma_{i,j,s-t}$$

where  $u = (s - 1)m + i$  and  $v = (t - 1)m + j$  for  $i, j = 1 \dots m$  and  $s, t = 1 \dots n$ .

The returned array `prest` is identical to  $\mathbf{x}$  except that the missing (unknown) values are replaced by their minimum error variance linear predictions (or projections) from the supplied (known) values.

The returned array `prvar` is identical in size to  $\mathbf{x}$  and contains, where  $\mathbf{x}$  had missing values, the (minimum error) variance of those values. Elsewhere, the elements of `prvar` are set to zero.

The returned array `Lincoef` is square of size  $mn$  with elements `Lincoef(i,j)` that are the elements of a matrix  $L$ . If  $\tilde{X}$  is the vector  $X = (x'_1, x'_2, \dots, x'_n)'$  with the unknown values set to zero, then  $\hat{X} = L \tilde{X}$  has the same structure but with the missing values set to their predictions and the known values set to zero. Thus  $L$  contains the linear coefficients of the missing values in terms of the known, and is elsewhere zero.